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ENGINEERING MECHANICS. VOLUME 1: EQUILIBRIUM

Latin capitals

Quantity		SI unit
Symbol	Name	Symbol ¹
Α	Work	Nm (J)
Α	Area	m ²
A _h	Horizontal component of the support reaction at A^2	N
A _m	Fixed-end moment at A ²	Nm
$A_{\rm v}$	Vertical component of the support reaction at A^2	Ν
$C_1; C_2$	Integration constants	-
$E_{\rm V}$	Strain energy	Nm (J)
F	Concentrated force, point load	N
\vec{F}	Force vector	Ν
Fa	Force along line of action a ³	Ν
F _h	Horizontal component of the force F	N
$F_{\rm V}$	Vertical component of the force <i>F</i>	N
$F_x; F_y; F_z$	Components of the force F	Ν
Fp	Prestressing force	Ν
G	Gravitational load	Ν
Н	Horizontal component of the cable force	N

Quantity		SI unit
Symbol	Name	Symbol ¹
М	Bending moment	Nm
Mt	Torsional moment	Nm
M_y	Bending moment in the xy plane	Nm
M_{z}	Bending moment in the xz plane	Nm
Ν	Normal force	Ν
R	Resulting force, resultant	Ν
Т	Concentrated couple (external moment)	Nm
\vec{T}	Moment vector of a couple	Nm
T_X	Moment about the x axis	Nm
T_y	Moment about the y axis	Nm
T_Z	Moment about the z axis	Nm
V	Shear force	Ν
V	Vertical component of the cable force	N
V_y	Shear force in the <i>xy</i> plane	Ν
V_z	Shear force in the <i>xz</i> plane	Ν

Latin lower case letters

Quantity SI unit		
Symbol	Name	Symbol ¹
а	Distance, length	m
а	Acceleration	m/s ²
b	Distance, width	m
d	Diameter	m
d	Depth	m
đ	(non-standardised) direction vector	-
$d_x; d_y; d_z$	Components of the direction vector	-
е	Eccentricity	m
ep	Eccentricity of the prestressing force	m
ē	Unit vector	-
$e_x; e_y; e_z$	Components of the unit vector	-
ez	<i>z</i> coordinate of the centre of force in the cross-section	m
g	Distributed permanent load	N/m
g	Gravitational acceleration	m/s ²
g	Gravitational field strength	N/kg
h	Height	m
l	Span, length	m
т	Mass	kg
ñ	Unit normal vector	-

¹Expressed in the basic units. ²The kernel A refers to the location and could therefore also be B, C, etc.

³The index a refers to the line of action and could therefore also be b, c, etc.

Quantity		SI unit
Symbol	Name	Symbol ¹
$n_x; n_y; n_z$	Components of the unit normal vector	-
р	Surface load (pressure, stress)	N/m ² (Pa)
р	Rise or sag of the parabola at midspan	m
<i>p</i> k	Distance between parabola and chord at midspan	m
\vec{p}	Stress vector	N/m ² (Pa)
$p_x; p_y; p_z$	Components of the stress vector	N/m ² (Pa)
q	Line load	N/m
<i>q</i>	Distributed variable load	N/m
\hat{q}	Top value of the line load	N/m
q_x	Distributed load in the <i>x</i> direction (the direction of the member axis)	N/m
q_z	Distributed load in the z direction (a direction normal to the member axis)	N/m
r	Radius	m
\vec{r}	Location vector	m
$r_x; r_y; r_z$	Components of the location vector	m
S	Path length	m

Quantity		SI unit
Symbol	Name	Symbol ¹
t	Time	s
и	Displacement in the <i>x</i> direction	m
ū	Displacement vector	m
$u_x; u_y; u_z$	Components of the displace- ment vector	m
υ	Velocity	m/s
υ	Displacement in the y direction	m
w	Displacement in the z direction	m
x	Rectangular coordinate	m
у	Rectangular coordinate	m
z	Rectangular coordinate	m

¹Expressed in the basic units.

Greek letters

Quantity		SI unit
Symbol	Name	Symbol ¹
α	Angle	rad
β	Angle	rad
γ	Angle	rad
γ	Specific weight	N/m ³
θ	Angle, change in angle due to rotation	rad
ρ	(mass) density, specific mass	kg/m ³

	Quantity SI unit	
Symbol	Name	Symbol ¹
σ	Stress, normal stress	N/m ² (Pa)
σ _{ij}	Stress on a plane with the normal in the <i>i</i> direction (i = x, y, z), and acting in the <i>j</i> direction $(j = x, y, z)$; normal stress when $i = j$ and shear stress when $i \neq j$	N/m ² (Pa)
τ	Shear stress	N/m ² (Pa)
φ	Angle, change in angle due to rotation	rad
φ_X	Rotation about the x axis	rad
φ_y	Rotation about the <i>y</i> axis	rad
φ_{z}	Rotation about the z axis	rad

¹Expressed in basic units.

A number of other signs and sign combinations

Δ	Change, increase
ΔM	Increase in M
Σ	Summation symbol
$\sum T \mathbf{B} $	Moment sum with respect to point B
δ	Variation symbol
δA	Virtual work
δи	Virtual displacement
$\delta \varphi$	Virtual rotation
$F_{\rm A}^{\rm BC}$	Force F at A (sub-index) on body BC (upper index)